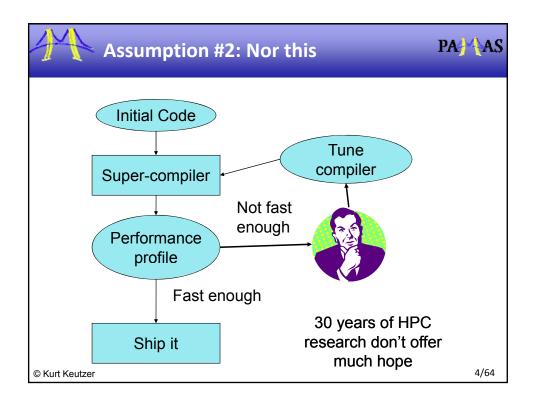
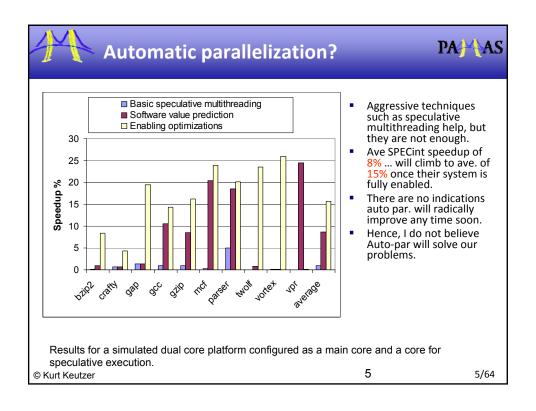
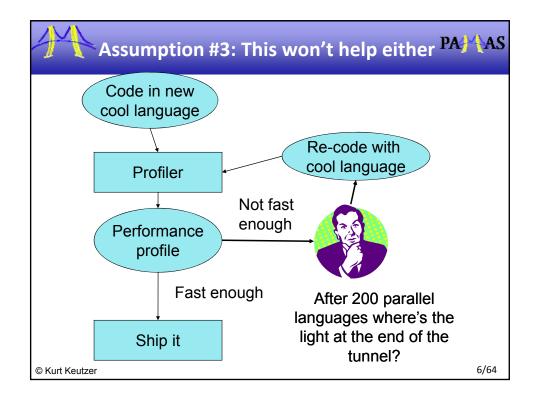
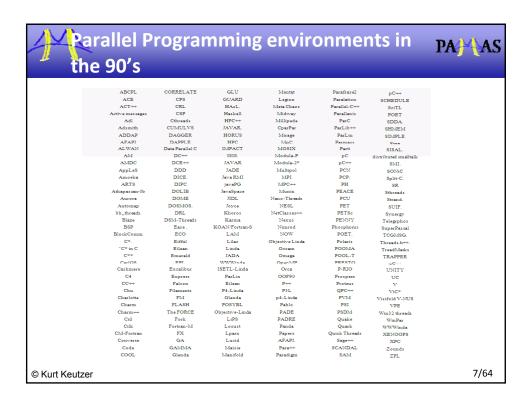


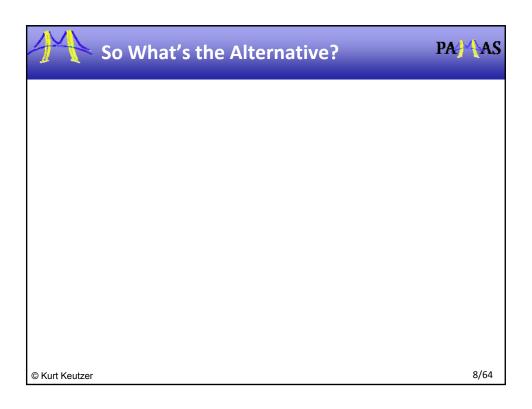
Steiner Tree Construction Time By Routing Each Net in Parallel							
Benchmark	Serial	2 Threads	3 Threads	4 Threads	5 Threads	6 Threads	
adaptec1	1.68	1.68	1.70	1.69	1.69	1.69	
newblue1	1.80	1.80	1.81	1.81	1.81	1.82	
newblue2	2.60	2.60	2.62	2.62	2.62	2.61	
adaptec2	1.87	1.86	1.87	1.88	1.88	1.88	
adaptec3	3.32	3.33	3.34	3.34	3.34	3.34	
adaptec4	3.20	3.20	3.21	3.21	3.21	3.21	
adaptec5	4.91	4.90	4.92	4.92	4.92	4.92	
newblue3	2.54	2.55	2.55	2.55	2.55	2.55	
average	1.00	1.0011	1.0044	1.0049	1.0046	1.004	













Principles of SW Design



- After 15 years in industry, at one time overseeing the techology of 25 software products, my two best principles to facilitate good software design are:
 - Use of modularity
 - Definition of invariants
- Modularity helps:
 - Architect: Makes overall design sound and comprehensible
 - Project manager:
 - As a manager I am able to comfortably assign different modules to different developers
 - I am also able to use module definitions to track development
 - Module implementors: As a module implementor I am able to focus on the implementation, optimization, and verification of my module with a minimum of concern about the rest of the design
 - Identify invariants and key computations

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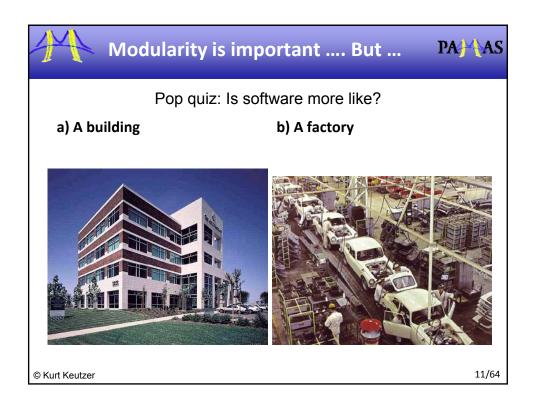


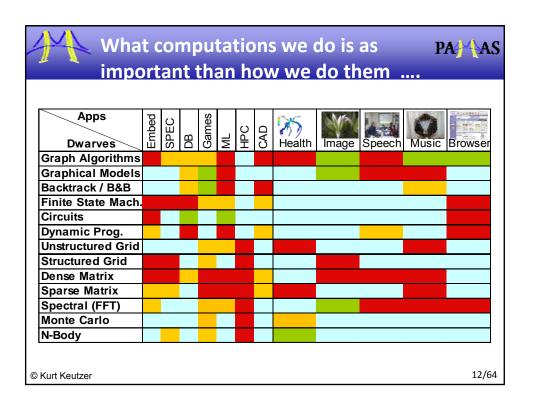
Non-Principles of SW Design



- What's life like without modularity?
 - Spaghetti code
 - Wars over the interpretation of the specification
 - Waiting on other coders
 - Wondering why you didn't touch anything and now your code broke
 - Hard to verify your code in isolation, and therefore hard to optimize
 - Hard to parallelize without identifying key computations
 - Modularity will help us obviate all these
 - Parnas, "On the criteria to be used on composing systems into modules," CACM, December 1972.

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Architecting Parallel Software

PA AS

- Putting computation and structure together:
 - We believe the key to productively building efficient and correct parallel software is software architecture
- A software architecture is a hierarchical composition of:
 - Computational patterns the atoms
 - Structural patterns the molecular bonds
- This software architecture naturally gives:
 - Modularity
 - Efficient management
 - Efficient implementation
 - Efficient verification
 - Identifies key computations, invariants, and interfaces

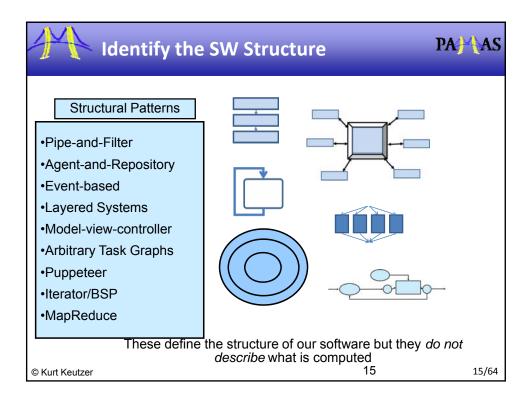
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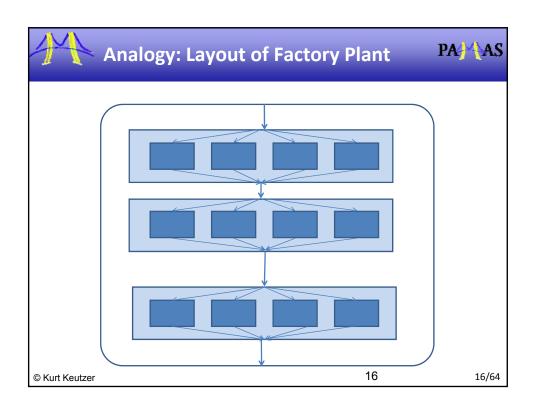


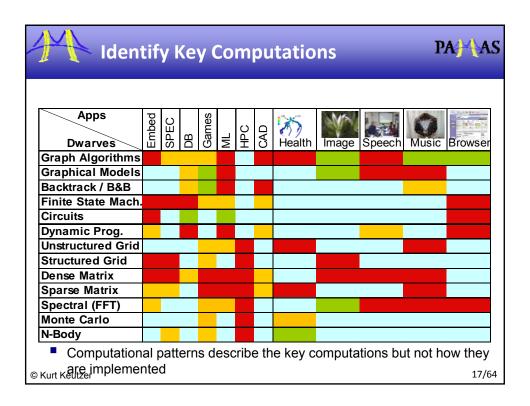
PA/\AS

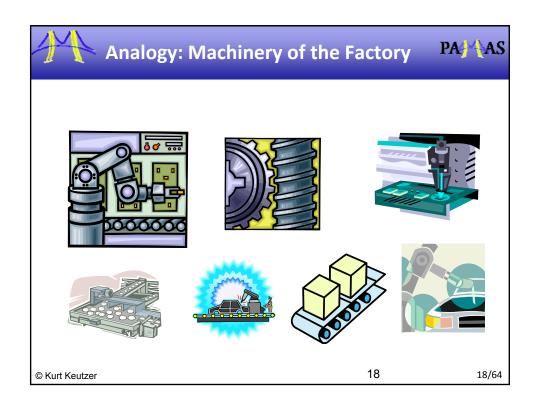
- Architecting Parallel Software
 - Structural Patterns
 - Computational Patterns
 - Examples
 - Summary

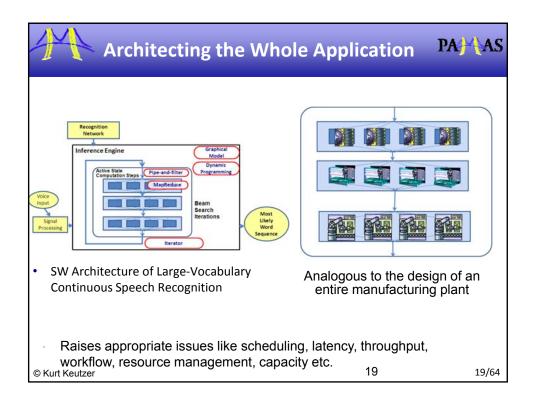
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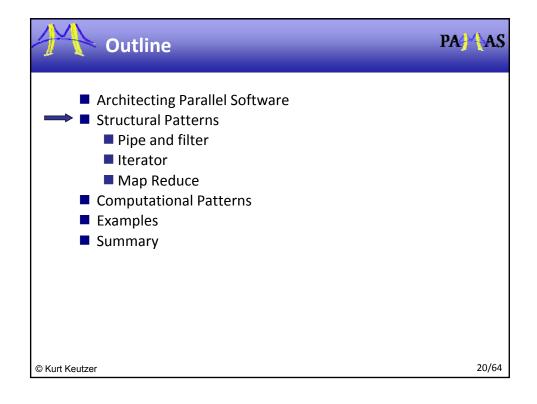


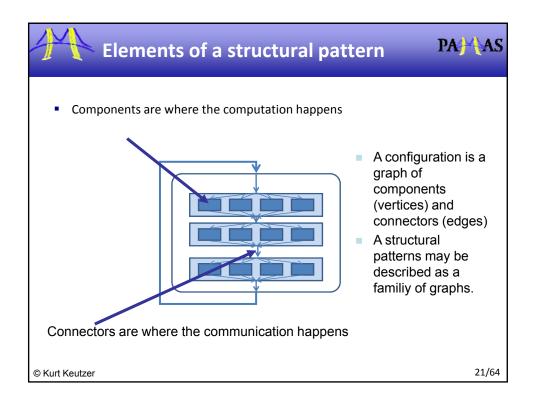


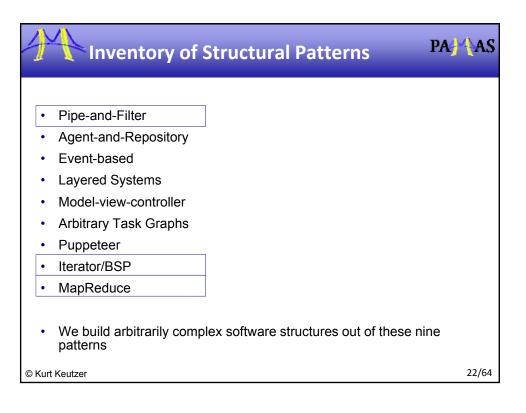


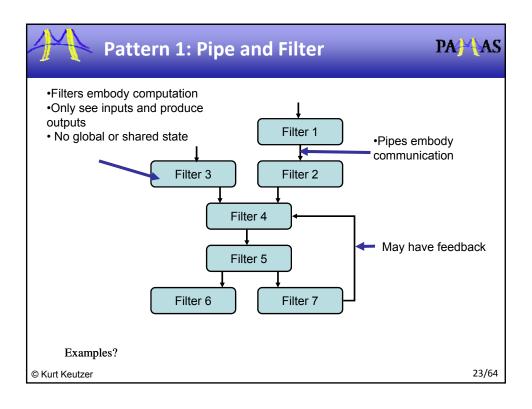


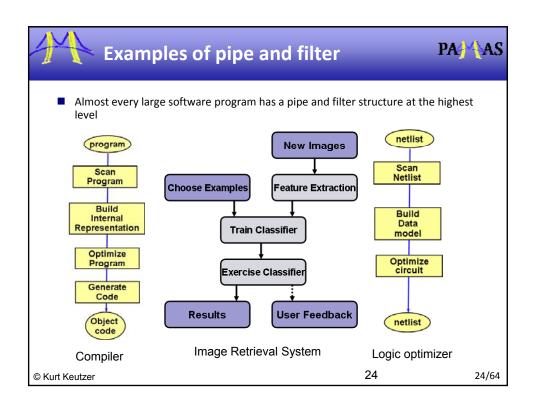


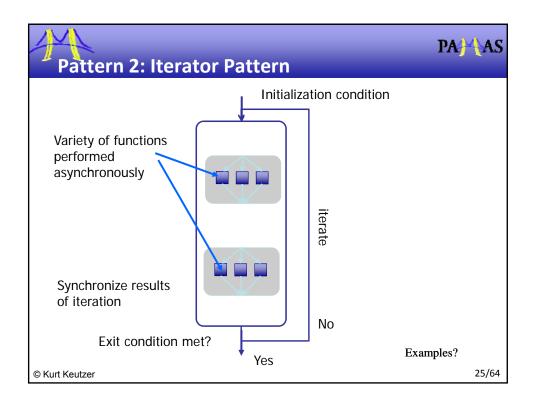


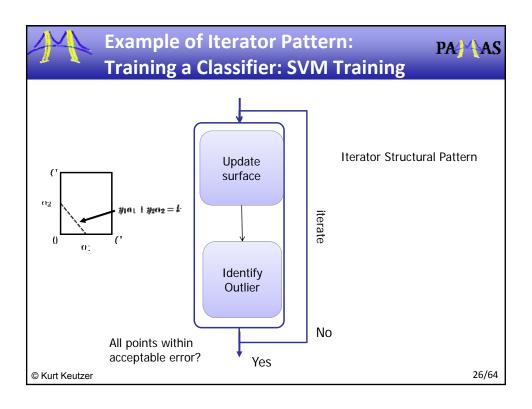


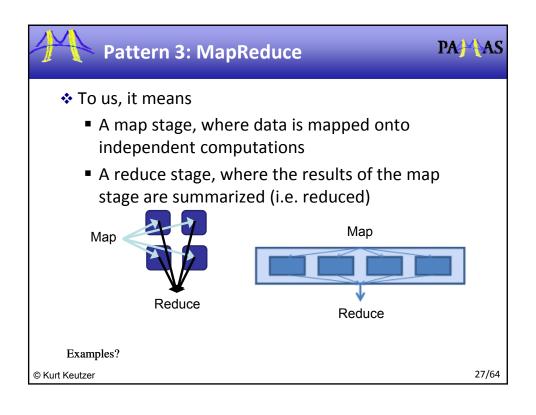


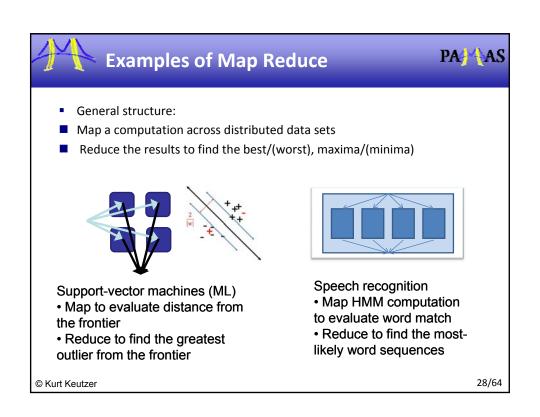


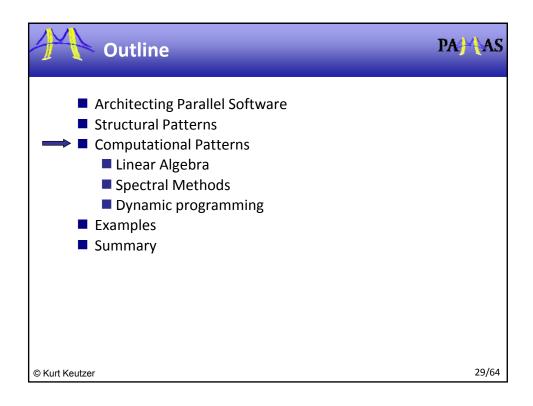


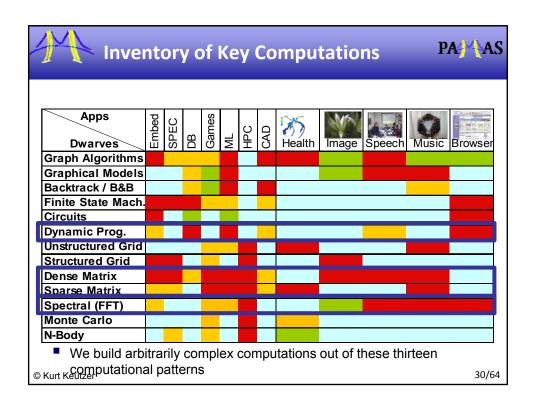














CP1: Linear Algebra

PA/\AS

- <u>Vector Space</u>: A set closed under + has identity and inverse elements, scalar multiplication
- <u>Linear Map</u>: Operator T on vectors u,v, scalar α s.t. T(u + v) = Tu + Tv, and $T(\alpha v) = \alpha T(v)$
- <u>Matrix</u>: An m × n array of numbers representing a Linear map from Rⁿ to R^m
- <u>Linear Equations</u>: Ax = b
- Eigenvalues/vectors: $Ax = \lambda x$

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Basic Linear Algebra Subroutines (BLAS)

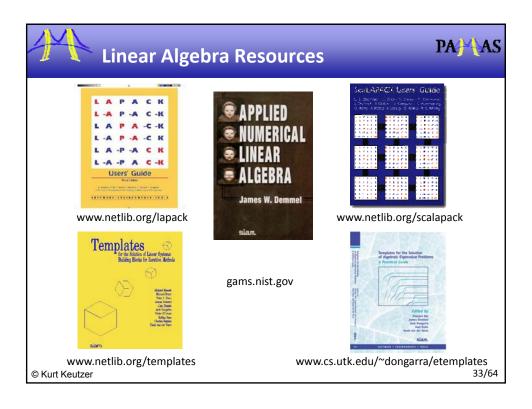


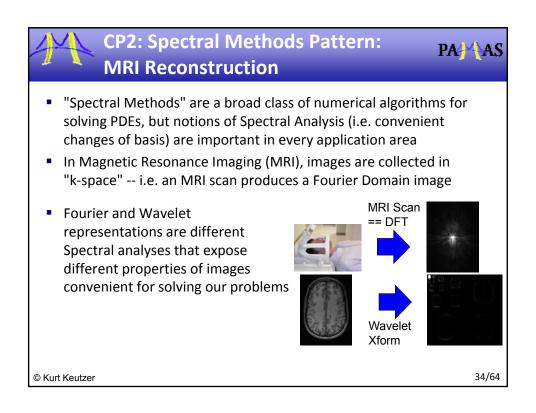
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 Three "Levels", known as BLAS, characterized by intrinsic ratio of computation to memory movement

Level	Example	# mem refs	# flops	q
1	$xAXPY: y = y + \alpha x$	3n	2n ¹	2/3
2	xGEMV: y=y+Ax	n ²	2n ²	2
3	xGEMM: C=C+AB	4n ²	2n ³	n/2

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Spectral Methods Pattern: Fast Transforms

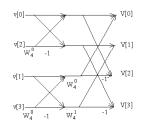


- Spectral Methods rely on representions of data in "convenient" bases that produce working, computationally feasible algorithms
- Changing a basis is, in general, an O(N²) matrix-vector multiplication. The matrices representing "convenient" bases factor into O(N log N) fast transforms!

$$y_k = \sum_{j=0}^{N-1} x_j \ \omega^{jk}$$

$$F = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & \omega & \omega^2 & \omega^2 \\ 1 & \omega^2 & \omega^4 & \omega^6 \\ 1 & \omega^3 & \omega^6 & \omega^2 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & -i & -1 & i \\ 1 & -1 & 1 & -1 \\ 1 & i & -1 & -i \end{bmatrix}$$

$$F_n \ x = \begin{bmatrix} I_{n/2} & D_{n/2} \\ I_{n/2} & -D_{n/2} \end{bmatrix} \begin{bmatrix} F_{n/2} \ x_{exen} \\ F_{n/2} \ x_{odd} \end{bmatrix}$$



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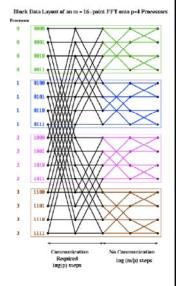
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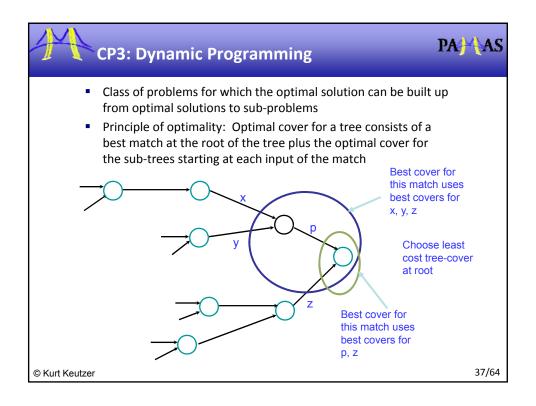
Spectral Methods Pattern: Libraries

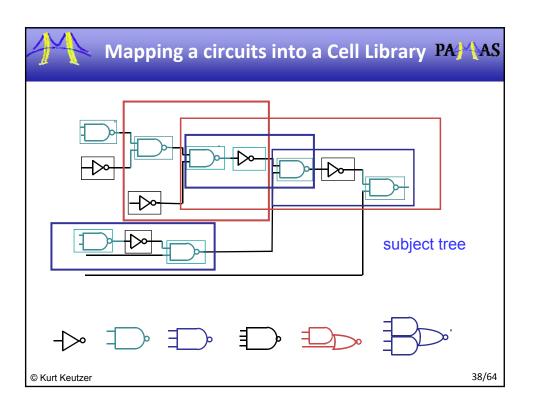


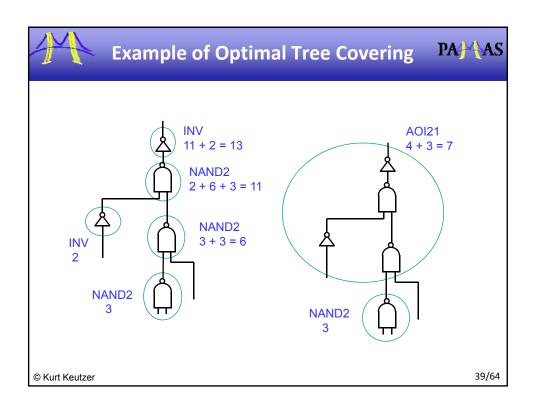
- Fast transform algorithms like the FFT are notoriously difficult to optimize:
- Luckily, implementations of the FFT exist for every platform. E.G:
 - FFTW and SPIRAL: Highly successful auto-tuners for FFT (and others) on PCs and workstations
 - CUFFT for Cuda on Nvidia GPUs

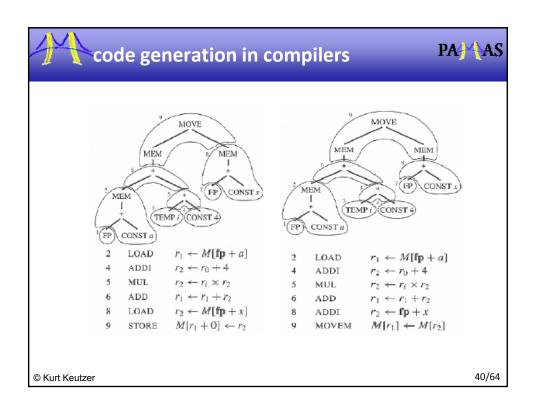


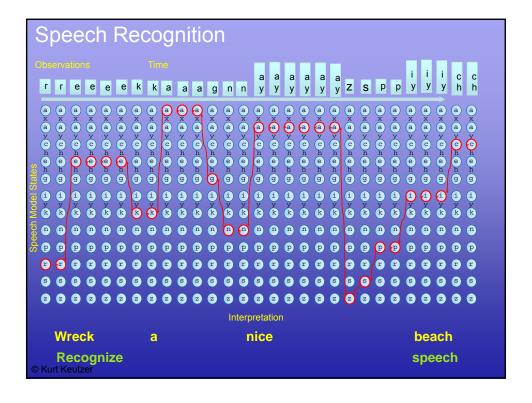
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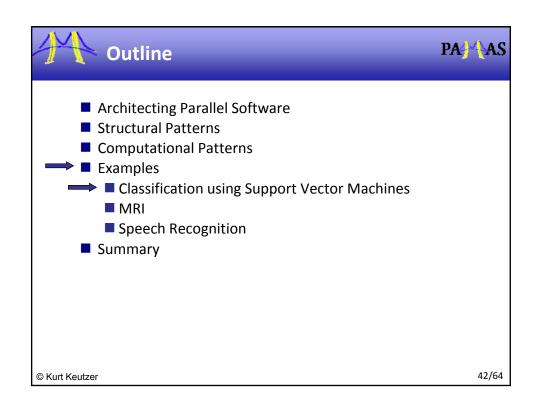


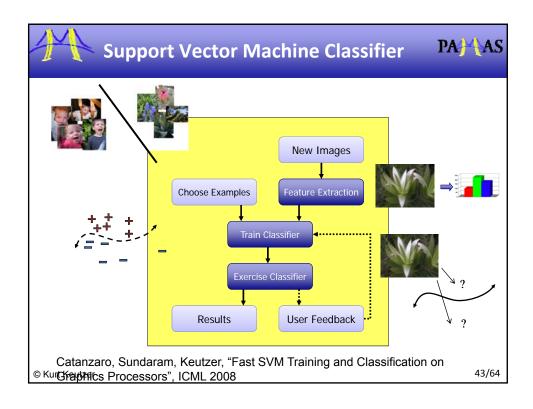


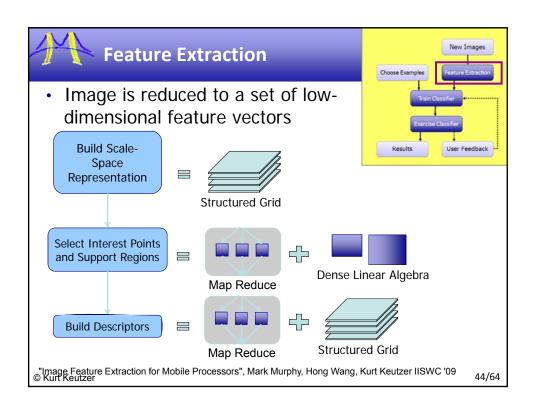


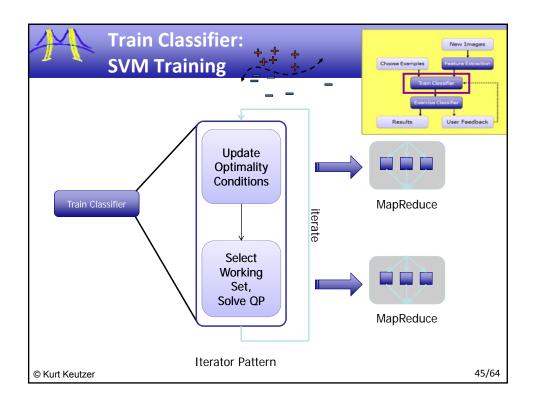


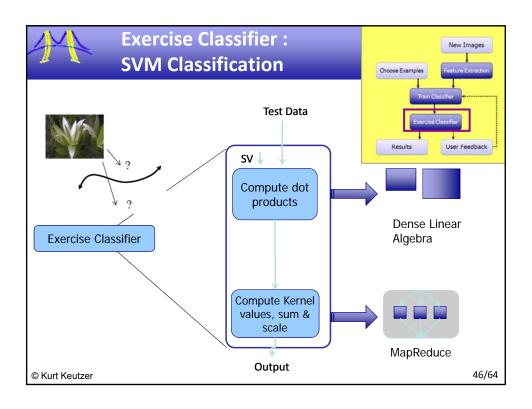


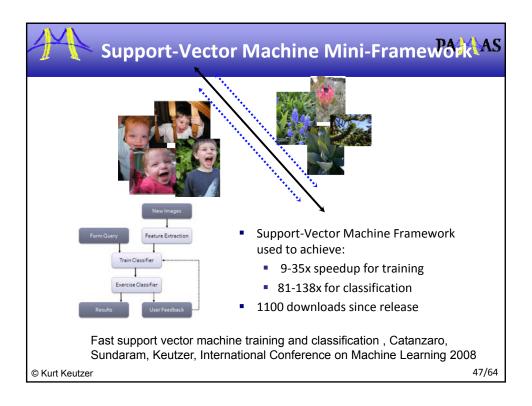


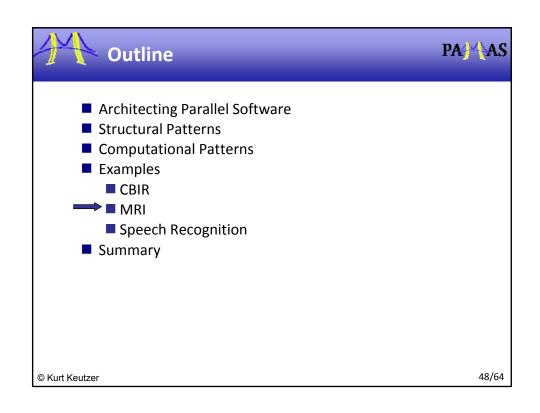








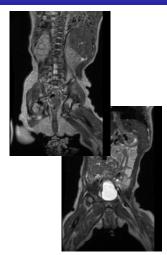




Compelling Application: Fast, Robust Pediatric MRI



- Pediatric MRI is difficult:
 - · Children cannot sit still, breathhold
 - Low tolerance for long exams
 - Anesthesia is costly and risky
- Like to accelerate MRI acquisition
 - Advanced MRI techniques exist, but require data- and compute- intense algorithms for image reconstruction
- Reconstruction must be fast, or time saved in accelerated acquisition is lost in computing reconstruction
 - Slow reconstruction times are a non-starter for clinical use



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Domain Experts and State-of-the-Art Algorithms



- Collaboration with MRI Researchers:
 - Miki Lustig, Ph.D., Berkeley EECS
 - Marc Alley, Ph.D., Stanford EE
 - Shreyas Vasanawala, M.D./Ph.D., Stanford Radiology
- Advanced MRI: Parallel Imaging and Compressed Sensing to dramatically reduce MRI image acquisition time





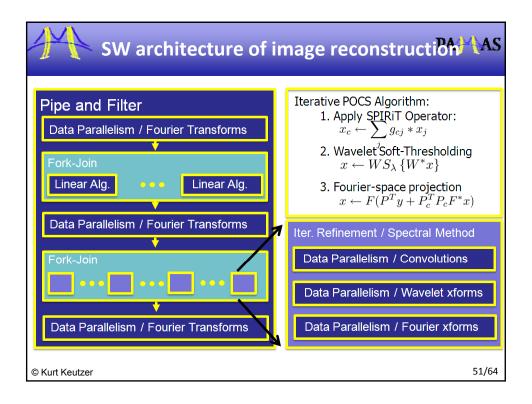


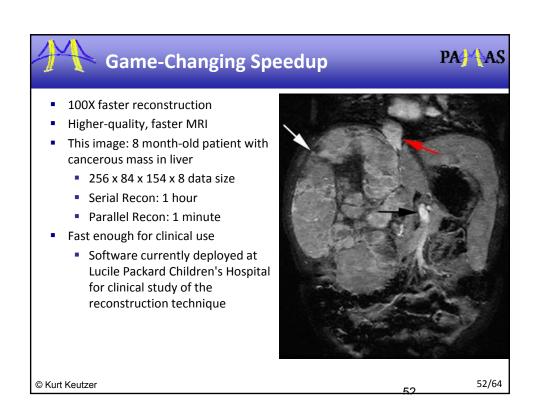


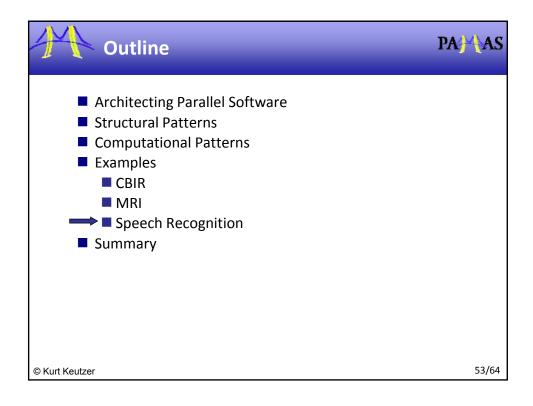
Computational IOU: Must solve constrained L1 minimization

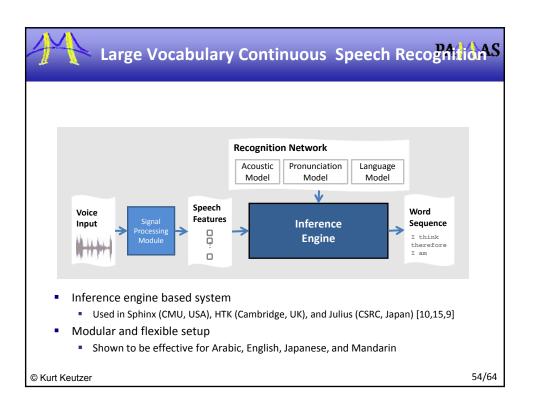
$$\begin{array}{ll} \text{minimize } ||Wx||_1 \\ \text{s.t} & \mathbf{F}_{\Omega}x = y, \\ ||\mathbf{G}x - x||_2 < \varepsilon \end{array}$$

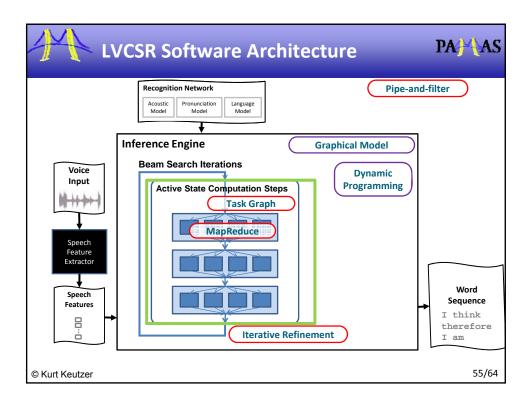
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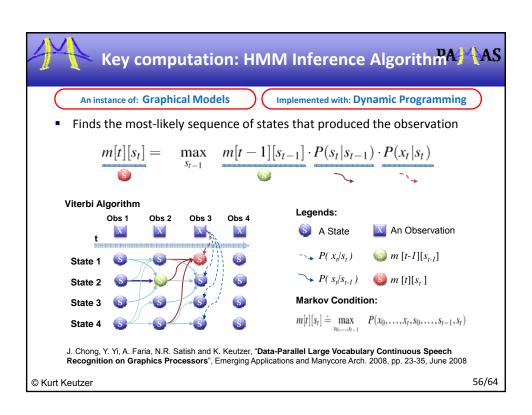


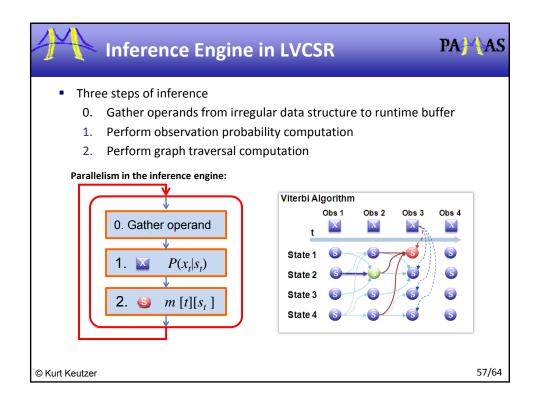


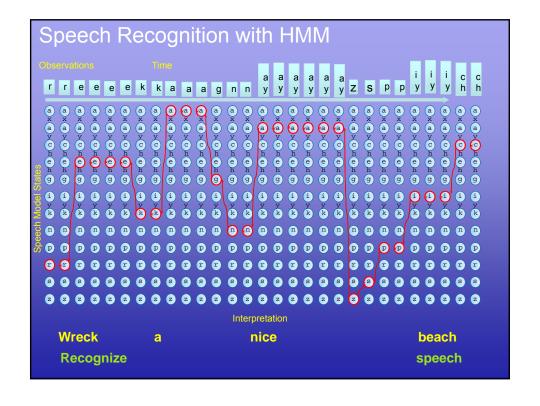


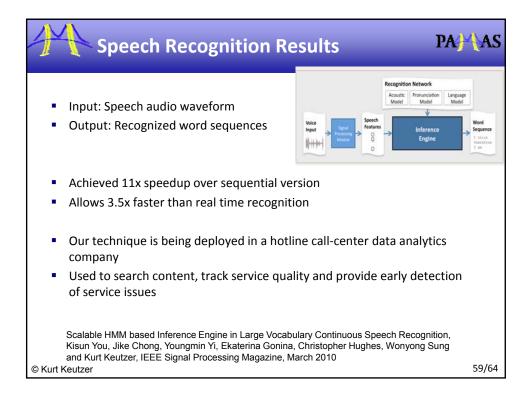


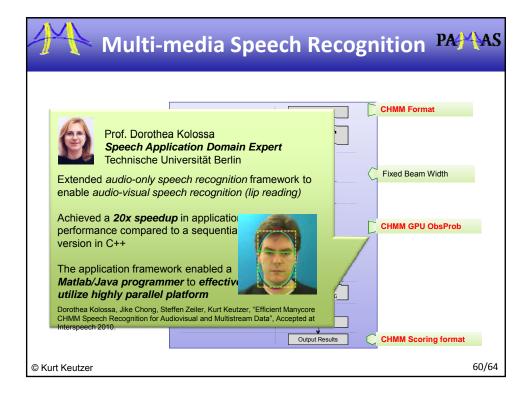


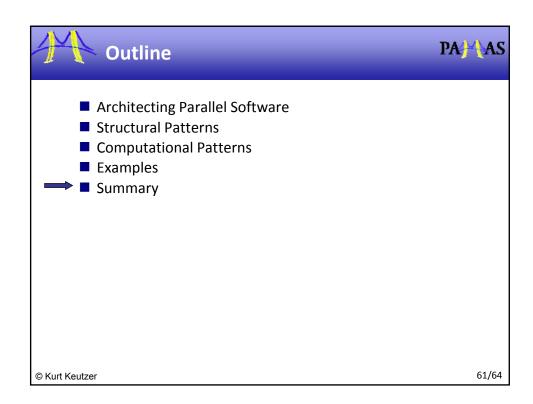
















- Patterns have helped the PALLAS research group publish papers in a diverse group of leading Computer Science conferences in the last few years:
 - Interspeech 2009, Interspeech 2010 (2)
 - IEEE Signal Processing Magazine 2009
 - European Conference on Computer Vision 2010
 - International Conference on Computer Vision 2009
 - Workshop on High Performance Computing in Finance at Super Computing 2009
 - Joint Annual Meeting of the International Society for Magnetic Resonance in Medicine, ISMRM 2010
 - International Conference on Machine Learning 2008
- What's the point?
 - Computational patterns give a new powerful viewpoint to efficiency programmers:
 - Enable us to disentangle the big fuzzy ball of yarn of computation
 - add 20 IQ points to our problem solving (as per Alan Kay)
 - Our Pattern language helps you to write good parallel code

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Summary

PA/\AS

- The key to productive and efficient parallel programming is creating a good software architecture – a hierarchical composition of:
- Structural patterns: enforce modularity and expose invariants
 - I showed you three –seven more will be all you need
- Computational patterns: identify key computations to be parallelized
 - I showed you three -ten more will be all you need
- Orchestration of computational and structural patterns creates architectures which greatly facilitates the development of parallel programs:
 - I showed you three there are *many* more

Patterns: http://parlab.eecs.berkeley.edu/wiki/patterns/patterns

PALLAS: http://parlab.eecs.berkeley.edu/research/pallas

CS194: Engineering Parallel Software: Fall 2010

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